RESEARCH ARTICLE

WILEY PRIMATOLOGY

Are great apes able to reason from multi-item samples to populations of food items?

Johanna Eckert[1,2] (iD) | Hannes Rakoczy[2] | Josep Call[1,3]

[1] Department of Developmental and Comparative Psychology, Max Planck Institute for Evolutionary Anthropology, Leipzig, Germany

[2] Department of Developmental Psychology, University of Goettingen, Goettingen, Germany

[3] School of Psychology and Neuroscience, University of St Andrews, St Andrews, United Kingdom

Correspondence
Johanna Eckert, Department of Developmental and Comparative Psychology, Max Planck Institute for Evolutionary Anthropology, Deutscher Platz 6, Leipzig 04103, Germany.
Email: johanna_eckert@eva.mpg.de

Inductive learning from limited observations is a cognitive capacity of fundamental importance. In humans, it is underwritten by our intuitive statistics, the ability to draw systematic inferences from populations to randomly drawn samples and vice versa. According to recent research in cognitive development, human intuitive statistics develops early in infancy. Recent work in comparative psychology has produced first evidence for analogous cognitive capacities in great apes who flexibly drew inferences from populations to samples. In the present study, we investigated whether great apes (*Pongo abelii*, *Pan troglodytes*, *Pan paniscus*, *Gorilla gorilla*) also draw inductive inferences in the opposite direction, from samples to populations. In two experiments, apes saw an experimenter randomly drawing one multi-item sample from each of two populations of food items. The populations differed in their proportion of preferred to neutral items (24:6 vs. 6:24) but apes saw only the distribution of food items in the samples that reflected the distribution of the respective populations (e.g., 4:1 vs. 1:4). Based on this observation they were then allowed to choose between the two populations. Results show that apes seemed to make inferences from samples to populations and thus chose the population from which the more favorable (4:1) sample was drawn in Experiment 1. In this experiment, the more attractive sample not only contained proportionally but also absolutely more preferred food items than the less attractive sample. Experiment 2, however, revealed that when absolute and relative frequencies were disentangled, apes performed at chance level. Whether these limitations in apes' performance reflect true limits of cognitive competence or merely performance limitations due to accessory task demands is still an open question.

KEYWORDS
comparative cognition, intuitive statistics, non-human primates, numerical cognition, probabilistic reasoning

1 | INTRODUCTION

Making general inferences from limited data is one of the key components of human inductive learning (see e.g., Denison & Xu, 2012; Holland, 1986; Tenenbaum, Griffiths, & Kemp, 2006; Skyrms, 1975). Traditionally, statistical reasoning was deemed to be difficult and error-prone (e.g., Cosmides & Tooby, 1996; Tversky & Kahneman, 1974, 1981) and dependent on language and formal education

(e.g., Piaget & Inhelder, 1975). However, recent studies suggest that even very young human infants have an astonishingly broad understanding of statistical relations: They are able to generalize from small samples to larger populations (Denison, Reed, & Xu, 2013; Xu & Garcia, 2008), make predictions about single event probabilities (e.g., Téglás, Girotto, Gonzalez, & Bonatti, 2007) and use these predictions to guide their search for desired objects (Denison & Xu, 2010b, 2014; Feigenson, Carey, & Hauser, 2002). In one remarkable

study, for example, infants were confronted with two jars containing mixtures of preferred and non-preferred types of candy (Denison & Xu, 2010b). After they had watched the experimenter randomly sampling one piece of candy from each jar and placing it in an occluded cup, most infants searched in the cup that contained a sample from the jar with a higher proportion of their preferred candy (Denison & Xu, 2010b). Hence, infants seem to have used the proportional information provided by the populations to reason about the samples. Moreover, infants can integrate probabilistic information with information from other domains such as intuitive physics or intuitive psychology (Denison, Trikutam, & Xu, 2014; Téglás, Vul, & Girotto, 2011; Denison & Xu 2010a; Xu & Denison 2009). For example, infants understand that a preference of the experimenter for a certain type of object can turn a sampling process into a non-random event. If the same experimenter, however, is blindfolded, infants expect the sampled objects to reflect the proportions within populations (Xu & Denison 2009). These findings imply that at least at the age of 6 months, humans already flexibly use intuitive statistics to predict the outcome of events. Being apparently independent of language or formal education, this raises the question whether these kinds of probabilistic reasoning represent an evolutionary ancient trait that is shared with other species.

Many species are capable of numerical cognition: For example, great apes (e.g., Beran, McIntyre, Garland, & Evans, 2013; Boysen & Berntson, 1989; Call, 2000; Hanus & Call, 2007), old- and new-world monkeys (e.g., Barnard, Hughes, & Gerhardt, 2013; Beran, Evans, Leighty, Harris, & Rice, 2008; Beran & Parrish, 2016), elephants (Perdue, Talbot, Stone, & Beran, 2012), bears (Vonk & Beran, 2012), raccoons (Davis, 1984), dogs (Ward & Smuts, 2007), cats (Pisa & Agrillo, 2009), birds [e.g., Rugani, Cavazzana, Vallortigara, & Regolin, 2013], fish [e.g., Potrich, Sovrano, Stancher, & Vallortigara, 2015], and even insects [bees: Dacke & Srinivasan, 2008; ants: Reznikova & Ryabko, 2011] are able to compare quantities, suggesting that representing numerosity is an evolutionary ancient trait. The practical advantages of such a capacity are obvious: in the context of foraging, for example, comparing quantities is a highly useful tool to identify the most profitable feeding location [see e.g., Farnsworth & Smolinski, 2006 and Hunt, Low, & Burns, 2008 for field experiments on quantity discrimination in a foraging context]. In the context of competition comparing ones own group size with that of a rival group can help to estimate the chances of winning a potential fight [e.g., Benson-Amram, Heinen, Dryer, & Holekamp, 2011; McComb, Packer, & Pusey, 1994; Wilson, Britton, & Franks, 2002]. Chimpanzees, for example, have been found to attack an opponent group only if their own group outnumbers those of their conspecifics by at least 1.5 (Wilson et al., 2002).

Relatedly, one can imagine that in some situations it would make sense for an animal to be able to make probability judgments instead of straightforward quantity comparisons. Efficient foraging, for instance, requires an individual to search for food in locations that most likely provide the best payoff in relation to foraging time (Geary, Berch, & Mann Koepke, 2015; for a review about optimal foraging theory see example, Hamilton, 2010). One possibility to identify the best payoff

per time unit is to use the relative frequency of past successes in a feeding location. Imagine a group of chimpanzees that has to decide in the morning in which direction to go: Either toward feeding ground A or toward feeding ground B. The apes might want to compare the proportion of times they visited each feeding ground and obtained a sufficient amount of food instead of simply comparing the absolute number of times they were successful in each location. Hence, non-human animals could clearly benefit from an ability exceeding a mere estimation of absolute or relative numerosity, namely a sense for probabilistic relations, that is, intuitive statistics. Future research will need to investigate both when and due to which selection pressures intuitive statistics evolved.

A recent comparative study investigated intuitive statistical abilities in non-human great apes with the same kinds of methods used in infancy research (Rakoczy, Clüver, & Saucke, 2014). Individuals of four great ape species were presented with two populations of food items. Both populations consisted of the same two types of food (one type clearly preferred over the other) but with different relative frequency distributions. The experimenter drew a one-object-sample from each population and gave the subject a choice between the two hidden samples. Hence, subjects had to infer which population was more likely to yield a preferred food item as a sample. Interestingly, individuals of all tested great ape species were able to form correct expectations about the probability of the sampling events, even when absolute and relative frequencies within the populations were disentangled. Apeś inferences were, therefore, not only based on information about absolute frequency, but instead they were truly based on probabilistic information. Most recently, another representative of the primate order was tested in the same paradigm: Capuchin monkeys Sapajus sp (Tecwyn, Denison, Messer, & Buchsbaum, 2016). In a series of four experiments, the monkeys were allowed to choose between the randomly drawn samples of two populations of food items with different proportions of preferred and non-preferred food. Results revealed that a few individuals might have drawn probabilistic inferences based on proportional information (control conditions excluded the usage of simpler choice heuristics). However, monkeyś performance in a baseline control condition was unexpectedly low, questioning whether they truly fully understood the procedure. It remains, therefore, an open question whether primates other than great apes are capable of intuitive statistics.

Although the findings of Rakoczy et al. (2014) raised the possibility that apes and human infants may operate with the same cognitive capacities for intuitive statistics, it leaves many open questions for future research. One fundamentally important question is whether apes' intuitive statistics reveal the same kinds of flexibility and generality as those found in human infants. In particular, does their ability to form expectations about samples randomly drawn from populations (inference population > sample; Rakoczy et al., 2014) extend to the ability to reason from a given sample to the corresponding population (inference sample > population)?

In human infants, this question was addressed using the violation of expectation (VOE) looking-time paradigm (Denison et al., 2013; Xu & Garcia, 2008). In one study (Xu & Garcia 2008) 8-month-old infants

were presented with boxes containing populations of red and white Ping-Pong balls. The distribution of red to white balls was either 9:1 or 1:9. During test-trials, the box containing one of the two populations of Ping-Pong balls was covered and the infants watched the experimenter drawing (apparently randomly) a sample of either four red and one white Ping-Pong balls or one red and four white Ping-Pong balls. Subsequently, the experimenter removed the cover of the box she had drawn from and revealed the population. Infants looked longer at the "mostly red"-sample when it was drawn from the "mostly white" population (unexpected) than when it was drawn from the "mostly red" population (expected). The analogue was true for the "mostly white"-sample. In a control condition it could be ruled out that infants simply reacted to the perceptual mismatch between sample and population: Instead of drawing the balls as samples from the box, the experimenter pulled them out of her pocked and placed them next to the box, resulting in equal looking-times at both matched and mismatched outcomes. This implies that, confronted with a sample, infants were able to make inferences about the associated population. Applying the same paradigm, a second study (Denison et al., 2013) showed that even 6-month-old infants had intuitions about relationships between samples and populations, suggesting that the ability to make inferences based on samples develops very early in human ontogeny. The results of these two infant studies (Denison et al., 2013; Xu & Garcia, 2008) together with the findings of the first study on intuitive statistics in great apes (Rakoczy et al., 2014) may indicate that the capacity of making inductive inferences is shared with other non-human species.

In the current study we tested great apes' ability to reason from samples to populations. Combining the methodology of Rakoczy et al. (2014) and Xu & Garcia (2008), we confronted apes with two covered containers holding populations of food items that differed in their proportion of preferred to neutral food (24:6 vs. 6:24). In two experiments, the apes witnessed the experimenter drawing one multi-item sample from each population. The distribution within the multi-item samples reflected the distribution of the respective populations (e.g., 4:1 vs. 1:4). Based on the observation of these representative samples, the apes were allowed to choose between the two covered populations. Hence, to receive the more favorable population, they were required to use proportional information provided by the samples. In Experiment 1 we tested whether apes were able to reason from samples to populations. In the crucial 4:1 versus 1:4 Test condition, apes were confronted with two populations (24:6 vs. 6:24) and watched the samples 4:1 versus 1:4 being drawn from them. Two control conditions were designed to rule out alternative explanations. In Control condition 1 apes did not see the available populations beforehand. This manipulation tested whether the information provided by the samples alone was sufficient for the apes to infer about the distribution within the populations. In Control condition 2, the samples were not re-inserted into the populations after the drawing process. This manipulation tested whether apes' success in previous conditions might have reflected a tendency to choose the population where the more favorable sample was inserted, without necessarily having to reason about the drawing process. In Experiment

2, apes were tested in two further Test conditions in which absolute and relative frequencies of preferred food items within samples were disentangled: In the 2:1 versus 4:8 Test condition, the absolute number of preferred food items was lower in the sample drawn from the more favorable population and therefore, misleading. In the 4:1 versus 4:8 Test condition, the absolute number of preferred food items was the same in both samples and therefore inconclusive. Hence, to receive the more favorable population in Experiment 2, apes had to take into account proportions, rather than absolute numbers.

2 | EXPERIMENT 1: CAN APES REASON FROM SAMPLES TO POPULATIONS?

In this experiment we sought to investigate whether apes were able to reason from multi-item samples to populations. In the Test condition, the experimenter presented the apes with two covered containers holding populations of food items (24:6 vs. 6:24). After watching representative samples being drawn from those populations (4:1 vs. 1:4), subjects were allowed to choose between the two containers. Two control conditions (1) tested whether apes inferred from the samples alone which distribution the populations had and (2) ruled out that subjects used the simple heuristic of choosing the container where the more attractive sample was inserted after the sampling process (see Figure 1 for an illustration of the different Test conditions). Based on the results of Rakoczy et al. (2014) we expected no inter-specific differences.

2.1 | Methods

2.1.1 | Subjects

Twenty-six individuals (female N = 20) of four great ape species participated: Gorillas (Gorilla gorilla, N = 4), Bonobos (Pan paniscus, N = 6), Chimpanzees (Pan troglodytes, N = 10), and Orangutans (Pongo abelii, N = 6). One further chimpanzee was tested but excluded from data analysis since he did not complete all sessions due to lack of motivation. Subjects were housed at the Wolfgang Koehler Primate Research Center (WKPRC) in the Leipzig Zoo and were tested between November 2014 and September 2015. Their age ranged between six and 48 years (Mean = 18 years) and about 25% were hand-reared. The remaining 75% were mother-reared (see Table 1 for more subject information). All apes were already experienced in participating in cognitive tasks with food-rewards as reinforcement. To control for potential order effects, 15 of the subjects underwent Experiment 1 first and then proceeded to Experiment 2, the remaining 11 subjects experienced Experiment 2 first and were tested in Experiment 1 afterwards (see Figure 2).

The study was ethically approved by an internal committee at the Max Planck Institute for Evolutionary Anthropology. Research and animal husbandry comply with the "EAZA Minimum Standards for the Accommodation and Care of Animals in Zoos and Aquaria," the "EEP Bonobo Husbandry Manual," the "WAZA Ethical Guidelines for the Conduct of Research on Animals by Zoos and Aquariums" and the "Guidelines for the Treatment of Animals in Behavioral Research and
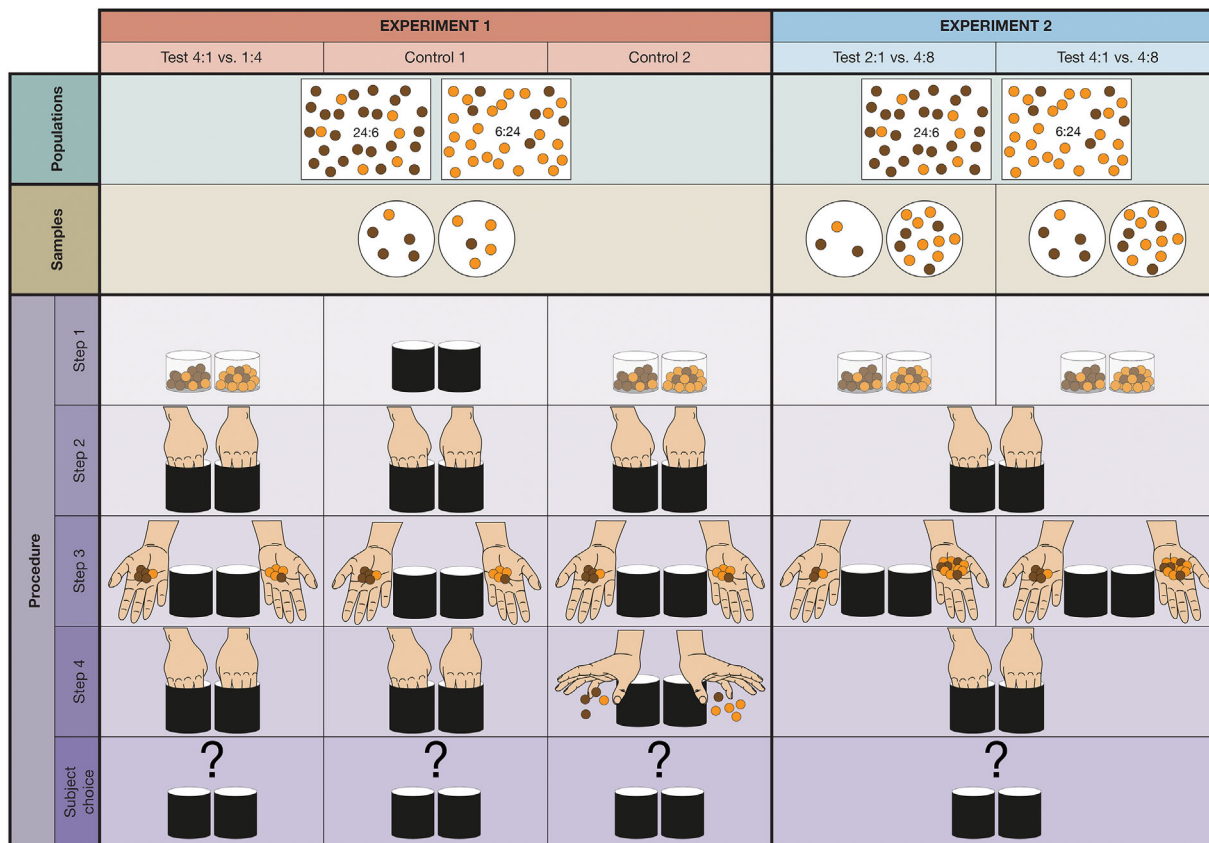
FIGURE 1 Schematic illustration of the different test conditions. Experiment 1 comprised one test and two control conditions. In Control 1, the populations were not shown prior to the sampling process. In Control 2, the samples were not replaced after sampling. The populations (24:6 vs. 6:24) as well as the samples (4:1 vs. 1:4) remained the same in all conditions of Experiment 1. Experiment 2 comprised two test conditions with the samples 2:1 versus 4:8 and 4:1 versus 4:8, respectively. The procedure and the populations remained the same as in the test condition of Experiment 1

Teaching" of the Association for the Study of Animal Behavior (ASAB). This research adhered to the American Society of Primatologists principles for the ethical treatment of primates.

2.1.2 | Materials

Subjects were tested individually in their sleeping cages or in special test cages. A Plexiglas panel fitted on the cage mesh separated ape and experimenter. The panel had two small holes (ø 2 cm; distance between holes 59 cm) through which subjects could insert a finger to indicate a choice. Perpendicular to the Plexiglas panel, a sliding table (45 × 79 cm) was mounted on the cage and could be moved both toward the subject and the experimenter. Underneath the table there were two small concealed compartments in which food items could be hidden prior to each test trial without the subject noticing it. To prevent subjects from watching, for example, preparation of a trial, a screen (27 × 79 cm) could be fixed via metal brackets at the end of the table closer to the ape's side. During test trials, apes were presented with two transparent Plexiglas containers (ø 8 cm), each containing a population of food items, namely pieces of fruit pellets and pieces of carrots of roughly equal shape and size. The containers could be covered with opaque

occluders of the same diameter that prevented subjects from seeing the content of the containers (see Figure 3 for an illustration of the setup).

2.1.3 | Design and procedure

Before the actual test started, subjects underwent a familiarization session. Subsequently, we carried out one test and two control conditions to investigate whether apes were able to reason from multi-item samples to populations. All conditions consisted of 12 test trials, divided into three sessions. Each session started with two preference trials with single pellet and carrot pieces (see Preference trials section). Thus, each session consisted of two preference trials and four test trials.

Familiarization

Each subject that had not experienced Experiment 2 before received one session with six trials of familiarization. In this session, the ape was confronted with one transparent container holding a population of carrot and pellet pieces (distribution 12:12). The experimenter presented the container to the ape, shook it several times to give a good overview of the population and subsequently placed it in the center of the sliding table.

TABLE 1 Detailed description of animals participating in this study

Subject	Species	Sex	Age	Rearing history	Start with experiment	Order of conditions	Drop out, reason
Fimi	Bonobo	F	7	Mother	2	Second	Yes, "covered population" follow-up
Gemena	Bonobo	F	9	Mother	2	Second	No
Kuno	Bonobo	M	18	Nursery	2	Second	No
Lexi	Bonobo	F	15	Nursery	1	First	No
Luiza	Bonobo	F	10	Mother	1	First	No
Yasa	Bonobo	F	18	Mother	1	First	No
Alexandra	Chimpanzee	F	15	Nursery	2	Second	No
Bangolo	Chimpanzee	M	6	Mother	1	First	Yes, lack of motivation
Daza	Chimpanzee	F	28	Unknown	2	Second	Yes, "open population" follow-up
Frodo	Chimpanzee	M	21	Mother	1	First	No
Jahaga	Chimpanzee	F	22	Mother	2	Second	No
Jeudi	Chimpanzee	F	48	Unknown	2	Second	Yes, "covered population" follow-up
Kara	Chimpanzee	F	9	Mother	2	Second	No
Lobo	Chimpanzee	M	10	Mother	1	First	No
Riet	Chimpanzee	F	37	Nursery	1	First	No
Robert	Chimpanzee	M	38	Nursery	2	Second	Yes, lack of motivation
Sandra	Chimpanzee	F	21	Mother	1	First	No
Tai	Chimpanzee	F	12	Mother	1	First	No
Abeeku	Gorilla	M	15	Mother	1	First	Yes, "covered population" follow-up
Kibara	Gorilla	F	10	Mother	1	First	No
Kumili	Gorilla	F	10	Mother	1	First	Yes, "covered population" follow-up
Viringika	Gorilla	F	19	Mother	1	First	No
Bimbo	Orangutan	M	34	Nursery	2	Second	No
Dokana	Orangutan	F	26	Mother	1	First	No
Padana	Orangutan	F	17	Mother	1	First	No
Pini	Orangutan	F	27	Mother	2	Second	No
Raja	Orangutan	F	11	Mother	2	Second	No
Suaq	Orangutan	M	6	Mother	1	First	No

During the first three trials the subject watched the experimenter drawing a random sample (three to five items) out of the population, presenting it on the palm of the hand, and re-inserting it into the container. After that, the experimenter moved the container to the edge of the table and pushed the sliding table forward, so that the ape could point to the container. Subsequently, the subject received the content of the container as reward. During the last three trials of familiarization, the procedure was the same as explained above, but this time the container was placed in an opaque occluder after the ape had seen the population. Thus, the subject did not see the population during the sampling process and when pointing to it. The familiarization should ensure that subjects were familiar with the material and that they understood that "inserting a hand in an occluded container" meant that a sample was drawn from the contained population.

Preference trials

The preference trials aimed at assuring the apes' constant preference for one of the two single-item types and were conducted prior to each of the test sessions. In each trial the experimenter placed one pellet piece and one carrot piece on the sliding table close to the Plexiglas panel, directly in front of the holes. The side on which the pellet piece was positioned was counterbalanced. Apes indicated their choice with their finger and immediately received the selected food item as reinforcement. Subsequently, the test trials of the respective condition were conducted. The criterion for an ape to be included in the analysis was choosing the pellet piece in at least 75% of the trials.

Test trials

All apes participated in three conditions. To control for a possible effect of order, 15 subjects were tested in the first order of conditions
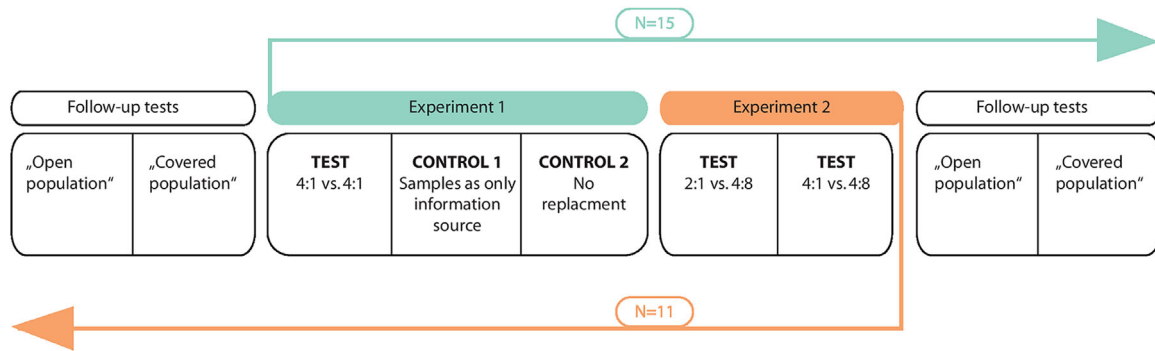
FIGURE 2 Schematic visualization of study design. Fifteen subjects were tested in the first order of conditions, starting with Experiment 1 through to Experiment 2. Eleven subjects were tested in the second order, starting with Experiment 2 through to Experiment 1. After completion of both experiments, subjects proceeded to the follow-up tests

(Test condition—Control 1—Control 2). The remaining eleven subjects were tested in the reverse order of conditions (Control 2—Control 1-Test condition). When we decided to split up subjects in the two groups of orders, all gorillas had already been tested in the first order of conditions. Thus, order was counterbalanced across subjects for all species except for the four gorillas, which were all tested in the original order of conditions (see Table 1 for information about the order of conditions each subject experienced). In all conditions, the populations consisted of 30 items each: Population A was composed of 24 pellet pieces and 6 carrot pieces; population B was composed of 6 pellet pieces and 24 carrot pieces. (These ratios were chosen because Rakoczy et al. (2014) showed that apes can reliably discriminate between multiples of the ratio 4:1 vs. 1:4. To not exceed the upper limit of caloric intake recommended for the apes, we had to limit the absolute number of food items to a certain extent. This limitation also

FIGURE 3 Experimental setup. The ape observed the experimenter drawing two representative multi-item samples out of two covered populations. Subsequently, the subject was given the choice between the two populations and received the content of the chosen container

reduced the risk of satiation and thereby helped to keep up apes' motivation over the course of trials).

Test 4:1 versus 1:4 In this condition the samples reflected the distribution of the populations one-to-one. More specifically, the sample apparently drawn from population A (24 pellets: 6 carrots) consisted of 4 pellet and 1 carrot pieces, and the sample apparently drawn from population B (6 pellets: 24 carrots) consisted of 1 pellet and 4 carrot pieces. Before a trial started, the experimenter fixed the screen on the table to prevent the subject from watching preparations. Subsequently, she positioned the pre-prepared multi-item samples in the small compartments underneath the table. The two containers holding the populations were placed next to each other in the center of the table and the two opaque occluders were positioned over them.

The trial started when the screen was removed from the sliding table unblocking the view over the table for the subject. The experimenter simultaneously removed the two occluders from the containers, and subsequently showed each population to the ape by lifting the container, tilting it forward and shaking it slightly. After the subject had seen both populations, the experimenter repositioned the occluders over the containers and put the screen back into the metal brackets. Then she shuffled both containers. Hence, subjects knew the two available populations, but did not know which population was which. Revealing the populations at the beginning of each trial ensured that apes were aware of both containers holding a relatively high number of food items (higher than the number of items subsequently drawn). During the shuffling process, the experimenter reached into the two compartments underneath the table, retrieved the hidden samples and put them into her fists to make sure that the subject did not see them there. After removing the screen again, the experimenter pretended to draw simultaneously out of each population by inserting her fists into the two covered containers and moving them around while looking upwards (maintaining a pretence of random drawing). While the subject was watching, she simultaneously removed both hands out of the containers and presented the samples on the palms of her hands close to the Plexiglas panel saying "look!". After the ape had seen
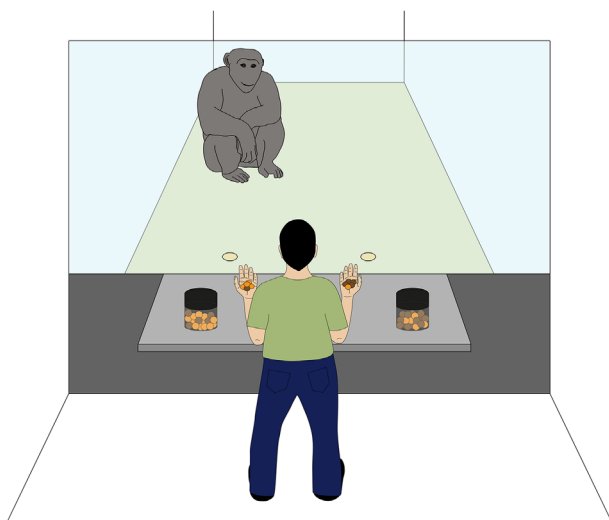
both samples, the experimenter let them fall back into the containers. Subsequently, the experimenter closed her eyes to minimize unintended cueing and pushed the sliding table slightly forward so that each container, covered by an occluder, was positioned directly in front of one of the holes. By inserting a finger into one of the holes, the ape could indicate her choice, which was coded live by the experimenter after she had opened her eyes again. In cases where the subject pointed toward both containers, the sliding table was pulled backwards with the words "just one," and then pushed forward again, giving the ape a new choice between the populations. After the ape had made her decision, the occluder of the chosen container was removed, revealing the selected population. Finally, the subject received the chosen population (see Figure 1 for an illustration of the procedure).

Control 1: samples as only source of information   To investigate whether apes were able to infer from the samples alone which distribution the populations most likely had, we carried out Control 1, in which the subjects did not see the available populations prior to the sampling process. The procedure of Control 1 was the same as in the Test condition, with the following exception: In the beginning of the trials, the experimenter did not remove the two occluders from the containers, preventing the apes from seeing the two available populations. Instead, she shook the containers with the occluders consecutively, making sure that the apes were aware of something being in the containers, but leaving them in uncertainty about the exact content (see Figure 1 for an illustration of the procedure).

Control 2: no replacement of samples   One alternative explanation for subjects succeeding in the Test condition as well as in Control 1 could be that apes did not make inferences about the drawing process and the populations as a whole, but based their choices on the side where the "more attractive" sample was inserted. More specifically, apes could have tracked their preferred sample and chosen the population in which this sample was dropped in. To rule that out, we conducted Control 2, in which the samples were not re-inserted into the populations. The procedure was the same as in the Test condition, but instead of letting the samples fall back into the containers, the experimenter threw them away in a bucket next to the table. Thus, the apes were prevented from basing their choice on the side where the "more attractive" sample was inserted and could instead use the samples only as a hint for the composition of the populations (see Figure 1 for an illustration of the procedure).

Follow-up tests
A pre-requisite for the correct interpretation of results was that apes recognized and had a preference for the population containing a higher proportion of pellet pieces. Therefore, we conducted two follow-up tests. Each of them was tested within a single session consisting of four trials. Note that the follow-up tests were the last conditions subjects underwent in this study, that is, individuals that underwent Experiment 1 first, were tested in the follow-up tests after completion of Experiment 2. Subjects that were tested in Experiment 2 first, received the follow-up tests after completion of Experiment 1 (see Figure 2). This was to ensure that none of the subjects had any prior experience regarding the populations before starting the test.

"Open population"-test   In the "open population" test, apes were presented with the same populations as during test conditions (A 24:6; B 6:24). For each trial, populations were placed in transparent containers standing next to each other in the center of the sliding table. The experimenter shook both containers successively and tilted them forward to give a full view of the available populations. Once the ape had seen both populations, the experimenter positioned the containers on the edge of the sliding table, each in front of one of the holes. Subsequently, she pushed the table forward and the ape could indicate her choice by pointing through one of the holes and received the content of the chosen container. The criterion for an ape to be included in the analysis was choosing the population containing more pellets in at least 75% of trials.

"Covered population"-test   The procedure of the "covered population" test was the same as in the "open population" test, except the fact that the experimenter pulled opaque occluders on the containers after the subject had seen the content. Thus, when making a choice, the ape was prevented from seeing the two populations; instead she had to memorize the position of her preferred population for a few seconds. This second follow-up test with covered containers was conducted to test for the possibility that some apes might not have been able to choose the correct container throughout the test trials due to the fact that it was not visible when the choice had to be made. Subjects were considered successful when they chose the pellet-population in at least 75% of trials. Based on previous studies that have shown that apes can solve quantity discrimination tasks that require encoding and mental comparison of quantities [e.g., Beran, Beran, Harris, & Washburn, 2005; Call, 2000], we expected that apes would be able to cope with the type of stimuli occlusion involved in this test.

2.1.4 | Coding and data analysis

The apes' choice was coded live by the experimenter. A second blind observer coded 25% of the trials from video. Both raters were in excellent agreement ($K = 0.95$, $N = 168$). Data of five subjects (one bonobo, two chimpanzees, and two gorillas, see Table S1 for individual data) had to be excluded because those individuals did not reach criterion in the follow-up tests (see Follow-up tests section). No ape had to be excluded on the basis of the preference trials. Data of all conditions were analyzed separately using R (R Core Team, 2014). Subjects' choices were the dependent

measure and were defined as "correct" if the chosen container contained the population with the more favorable ratio of pellets to carrots (24:6). The apes' overall performance (percent correct across trials) was tested against chance level using a two-tailed one-sample t-test (R function t-test). The effect sizes were obtained applying the package "lsr" (Navarro, 2015). In addition, we tested apes' first trial performance against chance level using an exact binomial test (R function binom.test) to detect potential learning effects. In order to test whether performance differed between species we used a one-way ANOVA (R function aov). This was justified as residuals were normally distributed and homogenous as verified by visual inspection of residuals plotted against fitted values and qqplot. For Tukey's post hoc test we used the R function TukeyHSD.

2.2 | RESULTS AND DISCUSSION

2.2.1 | Test 4:1 versus 1:4

Apes as a group chose the more favorable population on average in 72% of trials (see Figure 4 and supplementary material Table S1 for individual data), significantly more often than predicted by chance (t (20) = 6.12, $p < 0.001$, 95%CI [0.64, 0.79], N = 21; Cohen's d = 1.34). This pattern was also visible in the first trial performance (Mean = 71 %; Binomial test: p = 0.04, N = 21; Cohen's g = 0.43). Hence, the apes' performance seems to reflect an intuitive capacity rather than a learning effect. We detected no difference between species (ANOVA: F (3, 17) = 0.2, df = 3, p = 0.895). These results suggest that all tested species of great apes were able to intuitively use the information provided by the samples to receive the preferred population, therefore giving a first hint toward apes being able to reason from samples to populations.

2.2.2 | Control 1: samples as only source of information

Apes as a group chose the more favorable population on average in 69% of trials (see Figure 4 and supplementary material Table S1 for individual data), which is significantly above chance level (t (20) = 5.20, $p < 0.001$, 95%CI [0.62, 0.77], N = 21; Cohen's d = 1.13). However, this

pattern was not found considering only the performance in the first trial (Mean = 52%; Binomial test: p = 0.5, N = 21). This is perhaps best explained by insecurity about the available populations. Control 1 was the only condition in which subjects did not know the two possible answers (i.e., the two available populations) before making their decision. Hence, in the very first trial they could not be sure whether both populations were of the same size or whether, for example, the population associated with the "worse" sample contained many more items than the population from which the "better" sample was drawn. Potentially, apes had to experience during the first trial that, even though they had not seen the containers' content, there were two different populations of food items with the same absolute quantity. The first trial data suggest that subjects did not necessarily expect the populations to be the same as in other conditions, making it unlikely that subjects had learned and remembered the composition of the populations during the previous session(s). We detected no difference between species (ANOVA: F (3, 17) = 0.99, df = 3, p = 0.421). In sum, these results show that the information provided by the samples was sufficient for the apes to infer about the distribution within the populations.

2.2.3 | Control 2: no replacement of samples

Apes as a group chose the more favorable population on average in 66 % of trials (see Figure 4 supplementary material Table S1 for individual data), which is significantly more often than expected by chance (t (20) = 4.97, $p < 0.001$, 95%CI [0.59, 0.73], N = 21; Cohen's d = 1.08). This pattern was also reflected in the first trial performance (Mean = 76%; Binomial test: p = 0.01, N = 21; Cohen's g = 0.52) and thus cannot be due to learning. In this condition we detected differences between species (ANOVA: F (3, 17) = 4.88, df = 3, p = 0.01, R^2 = 0.46). Tukey multiple comparison of means revealed that bonobos performed significantly worse than gorillas (Mean bonobos = 53%, N = 5; Mean gorillas = 88%, N = 2, p = 0.015). However, considering the fact that we could only include the data of two gorillas (compared to five bonobos) in the final analysis, it is questionable whether this result truly reflects differences between species, or rather random variation or individual differences between subjects. The findings of Control 2 rule out the possibility that the apes solved the task by means of a simple heuristic: "choose the container where the more attractive sample was inserted." Instead, apes seem to have considered the drawing process and inferred about the population as a whole.

In sum, the results of Experiment 1 show that all tested species of great apes were able to use information provided by multi-item samples to track their preferred populations, and they did so even when they did not know the composition of the populations beforehand (Control 1) and when samples were not replaced after drawing (Control 2). These findings suggest that great apes might engage in intuitive statistical inferences from samples to populations in a comparable way human infants do (Xu & Garcia 2008; Denison et al., 2013). However, an alternative explanation for these results could be that apes simply associated the preferable sample (i.e., the sample containing absolutely more pellets), with
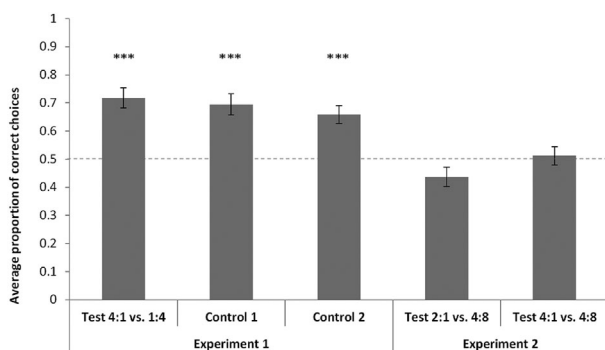

FIGURE 4 Mean proportion of trials (with standard errors) in which subjects chose the more favorable population. Dashed depicts chance level (50%)

the container that it was drawn from. To address this alternative explanation, we tested subjects in Experiment 2 with samples in which absolute and relative frequencies of pellets were disentangled.

3 | EXPERIMENT 2: DO APES TAKE INTO ACCOUNT RELATIVE, RATHER THAN ABSOLUTE FREQUENCIES?

Although results of Experiment 1 tentatively suggest that apes were able to reason from multi-item samples to populations, it is an open question to what extent the subjects relied on absolute quantities rather than on proportions to solve the task. More specifically, in all conditions of Experiment 1, absolute and relative frequencies were confounded within the samples, that is, the sample which contained the higher proportion of preferred food items than the alternative (4:1 vs. 1:4), also contained the higher absolute quantity of preferred food items (4 vs. 1). Thus, Experiment 1 alone cannot tease apart whether apes truly compared the proportion of pellets to carrots in both samples (4:1 vs. 1:4), or if they based their choice on the absolute amount of pellets (4 vs. 1) and used the heuristic: "choose the container where more pellets were drawn from." To address this question we tested apes in Experiment 2 in two further conditions. In both of them, absolute and relative frequencies within the samples were arranged in such a way that apes could not perform above chance level if they focused on absolute numbers only (see Figure 1 for an illustration of the Test conditions).

3.1 | Methods

3.1.1 | Subjects

The same 26 individuals as in Experiment 1 participated in this experiment. One additional chimpanzee was tested but excluded from data analysis as he did not complete all sessions due to a lack of motivation.

3.1.2 | Materials

We used the same materials as in Experiment 1 (see Figure 3 for an illustration of the experimental setup).

3.1.3 | Design and procedure

The general procedure was the same as in Experiment 1. To tease apart whether apes truly compared the proportion of preferred to neutral food items in both samples, or if they based their choice on the absolute amount of preferred food, we tested apes in two conditions with varying sample composition. Again, each condition consisted of 12 test trials, divided into three sessions. Prior to the test trials, two preference trials with single pellet and carrot pieces were carried out. Thus, each session consisted of two preference trials and four test trials.

Familiarization

Each subject that had not experienced Experiment 1 before received one session with six trials of familiarization. The procedure of the familiarization phase was exactly as described for Experiment 1.

Preference trials

The procedure of the preference trials was the same as in Experiment 1.

Test trials

All apes participated in two Test conditions. To control for a possible effect of order, 15 subjects were tested in the first order of conditions, starting with the 2:1 versus 4:8 test, through to the 4:1 versus 4:8 test. The remaining eleven subjects were tested in the reverse order of conditions (see Table 1 for information about the order of conditions each subject experienced). Again, in all conditions the populations consisted of 30 items each: Population A was composed of 24 pellet pieces and 6 carrot pieces; population B was composed of 6 pellet pieces and 24 carrot pieces

Test 2:1 versus 4:8

The procedure was the same as described for the Test condition of Experiment 1. However, the composition of the samples was varied in such a way that choosing the container from which the sample with the higher absolute number of pellets was drawn, resulted in receiving the less attractive population. In particular, the sample apparently drawn from population A (24 pellets: 6 carrots) consisted of 2 pellet and 1 carrot pieces, and the sample apparently drawn from population B (6 pellets: 24 carrots) consisted of 4 pellet and 8 carrot pieces. Thus, even though sample B contained double the amount of pellets compared to sample A, the proportion of pellets to carrots was more favorable in sample A. If apes' choice was based on absolute quantities, we expected them to choose the "wrong" container more often than the "correct" one. If they, however, took into account the proportion of pellets to carrots, we expected them to choose the "correct" container more often than the foil (see Figure 1 for an illustration of the procedure).

6.4.2 | Test 4:1 versus 4:8

Again, the procedure was the same as described for the Test condition of Experiment 1. However, here the composition of the samples was varied in a way that both samples contained the same absolute number of pellets. More specifically, the sample apparently drawn from population A (24 pellets: 6 carrots) consisted of 4 pellet and 1 carrot pieces, and the sample apparently drawn from population B (6 pellets: 24 carrots) consisted of 4 pellet and 8 carrot pieces. Assuming that apes based their choice on absolute quantities only, we expected them to choose both containers at similar rates, as the absolute number of

pellets did not provide any conclusive information. If they instead reasoned about the proportion of pellets to carrots, we predicted that they chose the correct container more often than expected by chance (see Figure 1 for an illustration of the procedure).

Follow-up tests

Those individuals that underwent Experiment 2 after Experiment 1 received the two follow-up tests. The procedure was exactly the same as described for Experiment 1.

3.1.4 | Coding and data analysis

The apes' choice was coded live by the experimenter. A second blind observer coded 25% of the trials from video. Both raters were in excellent agreement ($K = 0.95$, $N = 120$). Data of five subjects (one bonobo, two chimpanzees, and two gorillas, see Table S1 for individual data) had to be excluded because those individuals did not reach criterion in the follow-up tests. No further ape had to be excluded on the basis of the preference trials. Data analysis was the same as described for Experiment 1.

3.2 | Results and discussion

3.2.1 | Test 2:1 versus 4:8

Apes as a group chose the more favorable population on average in 44% of trials (see Figure 4 and supplementary material Table S1 for individual data). Though this pattern is not different from what was expected by chance (t (20) = −1.84, $p = 0.08$, 95%CI [0.36, 0.51], $N = 21$), it indicates a (non-significant) trend such that apes tended to choose the less favorable population more often than the more favorable one. We detected no differences between species (ANOVA: F (3, 17) = 1.66, df = 3, $p = 0.213$). This pattern was also reflected in the first trial performance (Mean = 47%; Binomial test: $p = 1$, $N = 21$). Hence, all tested species of great apes were unable to extrapolate from samples to populations, when the absolute number of preferred food-items was misleading. Instead, they tended to choose the population where the sample with the higher amount of preferred food-items was drawn from. This finding gives a first hint that the strategy applied by the apes might have been a comparison of absolute numbers between samples, rather than an extrapolation of proportions.

3.2.2 | Test 4:1 versus 4:8

Apes as a group chose the more favorable population on average in 51% of trials (see Figure 4 and supplementary material Table S1 for individual data), which is not different from chance level (t (20) = 0.37, $p = 0.715$, 95%CI [0.44, 0.58], $N = 21$). We detected no differences between species (ANOVA: F (3, 17) = 1.35, df = 3, $p = 0.292$). The same pattern was found considering only the performance in the first trial (Mean = 43%; Binomial test: $p = 0.664$, $N = 21$). This implies that apes failed to use the information provided by the samples to reason about

the populations and strengthens the theory that apes might have relied on absolute, rather than relative frequencies.

4 | GENERAL DISCUSSION

In Experiment 1, we investigated whether great apes are able to reason from multi-item samples to populations of food items. Results showed that great apes did extrapolate from samples to populations, irrespective of whether they knew the composition of the available populations beforehand or not (Control 1) and if samples were replaced after drawing or not (Control 2). The results of Control 2 are especially revealing, as they rule out the possibility of a simple heuristic: "choose the container where the more attractive sample was inserted". Instead, apes seem to have considered the drawing process and inferred about the population as a whole from the first trial onwards. This implies that apes seem to possess similar kinds of capacities as found in human infants (Xu & Garcia, 2008; Denison et al., 2013). In fact, our findings even go one step further than those of the two existing studies that tested infants' ability to reason from sample to population: While the apes in our study drew inferences from samples to populations in an active choice paradigm, the human infants in the above mentioned studies were only tested using the VOE looking-time paradigm. There is some evidence that findings of studies using the VOE looking time paradigm dissociate from findings of studies using active choice measures [e.g., Ahmed & Ruffman, 1998; Shinskey & Munakata, 2005; Charles & Rivera, 2009]. This is probably due to the fact that a subject that is able to perceive something is not necessarily able to act accordingly. As it is currently unknown whether human infants would succeed in an active choice paradigm testing for their capacities to reason from sample to population, we conclude that great apes' intuitive statistical abilities in this regard seem to be at least at a comparable level as those of young human infants. However, based on Experiment 1 alone it is impossible to rule out that apes used alternative strategies based on the absolute number of preferred food items. The aim of Experiment 2, therefore, was to investigate whether great apes can successfully reason from samples to populations when prevented from relying on absolute quantities. Apes performed at chance level both when the sample drawn from the more favorable population contained less preferred food items than the sample drawn from the less favorable population, and when both samples contained the same number of preferred food items. Thus, apes did not rely on inferences from samples to populations in this experiment. There are at least two interpretations for these findings.

One interpretation is that apes' failure in Experiment 2 reflects true limitations of their cognitive competences. The most obvious difference between Experiment 1 and 2 is that only in the latter subjects could not rely on absolute numbers of preferred food items. Hence, one could conclude that apes are able to reason and draw inferences about absolute, but not relative frequencies. Assuming that apes simply compared the absolute quantity of pellets in both samples and chose the population from which more pellets were drawn, we expected the following pattern of results: When the number of pellets

in the samples was inconclusive (because it was the same in both samples), apes should have chosen randomly between both populations. When the number of pellets was misleading, that is, higher in the sample drawn from the non-preferred population, apes should have chosen the "wrong" population more often. While apes indeed chose randomly between populations when the number of pellets was the same in both samples, they also did so when the number of pellets was misleading. Yet, it should be noted that even though there was no significant effect in this condition (misleading number of pellets in both samples), apes nevertheless revealed a non-significant tendency to choose the more favorable population less often than the more favorable one. Consequently, it cannot be ruled out that apes mainly relied on absolute quantities in this experiment.

This opens up an alternative explanation for the apes' success in Experiment 1: Subjects might have not drawn any inference from sample to population, but instead simply associated the more favorable sample (i.e., the one containing absolutely more preferred items than the other) with the container it was drawn from, since it was temporally and spatially most closely associated with that container. In other words, apes might have followed a heuristic like "chose the container where you saw something good (i.e., more pellets) coming from." Future studies need to determine whether subjects truly relied on associating containers with "better" and "worse," or if they in fact perceived the samples as a representation of populations. One possible way to disentangle the two explanations would entail presenting apes with two opaque containers filled with two populations of food items (similar to the current study). Crucially, the experimenter would already have the samples in her hands (i.e., pellets and carrots in 4:1 distribution in one hand, 1:4 in the other). She would then show the contents of her hands to the ape, insert her hands into the containers and remove them again, showing the same items as before. Subsequently, she would discard the samples and give the apes the choice between the two containers. If apes merely associated the two containers with "good" or "bad" according to the distribution they had seen on each side, we would expect them to choose the side where the sample with absolutely more pellets was shown. In contrast, if they recognized a randomly drawn sample as representation of the population, they should pick both containers equally often since no drawing took place, and therefore, no inference can be made.

Recall that Rakoczy et al. (2014) showed that great apes did take proportions into account when reasoning the other way around, that is from populations to samples, ruling out that subjects used a simple association mechanism to solve the task. If our results reflected true limitations in apes' cognitive competences, they would, therefore, suggest that nonhuman primates' statistical abilities could be unidirectional. This would question whether apes have a true understanding of drawing processes and the relation between populations and samples.

A different interpretation for the negative findings of Experiment 2 is that they may merely reflect performance limitations imposed by the task's cognitive demands, which may have masked

apes' true competence. One of these task demands could be the memory component required by our procedure. At the exact moment when apes were asked to make a choice, the information necessary to do so (i.e., the samples) was not available anymore. Instead, apes had to memorize this information for a few seconds and recall it to choose between the two populations. Note that this was not the case in Rakoczy et al. (2014), where subjects were still able to see the populations during their choice. Even though it may seem trivial to remember information for a few seconds, results of the follow-up test with covered populations showed that this was indeed a crucial factor for some of the subjects: Four of the 26 subjects were not able to choose the more attractive population when it was covered while the decision was made, even though they showed a clear preference for that population during the preference test with open populations. Furthermore, other studies have shown the importance of working memory in different problem solving tasks. For instance, in Seed, Seddon, Greene, and Call (2012) four chimpanzees solved a tool-use task requiring causal inferences when the time-span over which information had to be memorized was minimized. By contrast, in a related previous study (Povinelli, 2000) that involved a higher working memory load, all chimpanzees failed to do so. Although working memory demands, potentially in combination with lack of attention, may have influenced the apes' performance to a certain extent, working memory alone cannot fully explain the fact that apes were not able to use proportional information in this experiment. Recall that those subjects who had difficulties remembering the populations' position were excluded from the analysis and did therefore not bias the results in a negative way. Moreover, Experiment 1 also required a memory component, and still subjects succeeded.

Another factor that could have made this task more difficult as compared to Rakoczy et al. (2014) is the type of inferences required. Retrospective inferences seem to be harder than prospective ones (Völter & Call, 2017). This means that going from samples back to populations (retrospective) may be more demanding than going from populations forward to samples (prospective). The majority of knowledge that we have about the origin and development of intuitive statistics derives from the extensive study of pre-verbal infants. In the last decades, numerous such studies have tested infants both for their abilities in reasoning from populations to samples as well as from samples to populations. As mentioned above, to our knowledge there is no study testing pre-verbal infants for their ability to reason from samples to populations in an active choice measure. This type of methodology was, so far, only used in studies investigating infants' capacity to reason from population to sample (Feigenson et al., 2002; Denison & Xu, 2010b; Denison & Xu, 2014). In these studies, infants were allowed to choose between the covered samples of two populations of preferred and non-preferred items in different ratios. Control conditions disentangled absolute and relative frequencies with the result that infants indeed used proportional information, not a comparison of absolute quantities, to retrieve their preferred item. The two existing studies

investigating the reverse ability, that is, reasoning from samples to populations (Xu & Garcia, 2008; Denison et al., 2013), both used a VOE looking-time paradigm, a methodology that is less comparable with the methodology applied for great apes. Moreover, in both above-mentioned studies probability was confounded with quantity, and no control condition tested for the fact that infants could have used the shortcut of focusing on absolute quantities only. As a consequence, it remains unclear whether reasoning from samples to populations represents a cognitively more challenging task than the other way around. It would be of great interest to fill that gap of knowledge by applying an active choice paradigm to investigate pre-verbal infants' ability to reason from samples to populations, including a control condition for absolute versus relative information.

A third task demand that may have masked apes' true competence in Experiment 2 is the poorer discriminability of the samples as compared to the samples used in Experiment 1. As an index for discriminability we calculated the ratio of ratios (hereafter: ROR) of the two samples for each of the conditions in the following way [following Drucker, Rossa, & Brannon, 2016]:

$$\frac{\text{Ratio of pellets to carrots in the sample drawn from the preferred population}}{\text{Ratio of pellets to carrots in the sample drawn from the non-preferred population}}$$

In all conditions of Experiment 1, the ROR was (4/1)/(1/4) = 16 (in Rakoczy et al., 2014 the ROR was ≥16 in all conditions). In Experiment 2, the ROR was (2/1)/(4/8) = 4 in the 2:1 versus 4:8 test, and (4/1)/(4/8) = 8 in the 4:1 versus 4:8 test. Thus, in both conditions of Experiment 2, the ROR was less than or equal to half the one used in Experiment 1. This discrepancy was caused by our methodological constraints that prevented us from using larger RORs. More specifically, a larger ROR would have required larger samples and thus larger populations. As the apes received the "whole" chosen population as reinforcement we had to minimize the number of food items within the populations for the purpose of not exceeding their allowed daily caloric intake. Moreover, given that the food items were kept in the experimeter's fist, larger samples would have required a different sampling method than the one applied here. As a consequence, in this study it was not possible to disentangle absolute and relative information with the same ROR as in Experiment 1. Recent research suggests that indeed the magnitude of difference between two proportions is crucial for non-human primates to discriminate probabilities. Hanus & Call (2014) presented chimpanzees with two trays, each of them with a different ratio of hidden food items to potential hiding locations and therefore a different likelihood of finding food. This study revealed that subjects' performance was influenced by the relative difference between the two probabilities as soon as a certain threshold thereof was reached. Moreover, the apes relied on the ratio between probabilities, even in conditions where one tray depicted an absolute safe option—a probability of finding food of 100%. This study emphasizes the importance of the magnitude of difference between the two ratios to be discriminated, rather than the magnitude of difference within the single ratios.

With regard to the present study this means the following: Although the quantities within one sample were presumably easy to discriminate [for reviews about quantity discrimination see example, Feigenson, Dehaene, & Spelke, 2004; Nieder, 2005], it was probably the ratio between the ratios of both samples that influenced the decision of the apes and it could well be that the present RORs were simply below the threshold for discriminating two ratios and thus failed to constitute notable differences. In a study using a touch screen setup (Drucker et al., 2016) rhesus macaques (*Macaca mulatta*) were presented with arrays containing different ratios of positive to negative stimuli. The monkeys learned to choose those arrays with the greater ratio of positive to negative stimuli and were able to generalize to novel ratios. Similarly, as in the previously mentioned study with chimpanzees (Hanus & Call, 2014), the performance was directly influenced by the magnitude of difference between the two ratios to be discriminated. Interestingly, just as human infants (McCrink & Wynn, 2007), the two macaques tested were able to discriminate a ROR of 2, which is much lower than those used in our experiments. However, given the fact that those subjects received extensive training in such discrimination tasks before the actual test, it remains unclear to which extent those methods are comparable to the ones used here with apes.

5 | CONCLUSIONS

The aim of the current study was to investigate whether apes can use samples of items to infer the composition of the population from where the samples came from. While apes performed competently when the samples from the more favorable population were more attractive than the samples from the less favorable population not only in terms of relative but also in terms of absolute frequencies of preferred over non-preferred food items, they failed to do so when absolute and relative frequencies were disentangled. The present study, therefore, cannot determine whether non-human primates engage in intuitive statistical inferences from randomly drawn samples to populations in a comparable way human infants have recently been found to do (Denison et al., 2013; Xu & Garcia, 2008). It is an open question for future research whether these limitations in apes' performance reflect true limits of cognitive competence or merely performance limitations due to accessory task demands.

CONFLICT OF INTEREST

None.

ORCID

Johanna Eckert http://orcid.org/0000-0001-8161-0828

REFERENCES

Ahmed, A., & Ruffman, T. (1998). Why do infants make A not B errors in a search task, yet show memory for the location of hidden objects in a nonsearch task? *Developmental Psychology*, 34(3), 441–453.

Barnard, A. M., Hughes, K. D., & Gerhardt, R. R., DiVincenti, L., Bovee, J. M., & Cantlon, J. F. (2013). Inherently analog quantity representations in olive baboons *(Papio anubis)*. *Frontiers in Psychology*, 4, 253.

Benson-Amram, S., Heinen, V. K., Dryer, S. L., & Holekamp, K. E. (2011). Numerical assessment and individual call discrimination by wild spotted hyaenas, *Crocuta Crotua*. *Animal Behaviour*, 82, 743–752.

Beran, M. J., Beran, M. M., Harris, E. H., & Washburn, D. A. (2005). Ordinal judgments and summation of nonvisible sets of food items by two chimpanzees *(Pan troglodytes)* and a rhesus macaque *(Macaca mulatta)*. *Journal of Experimental Psychology: Animal Behavior Processes*, 31, 351–362.

Beran, M. J., Evans, T. A., Leighty, K. A., Harris, E. H., & Rice, D. (2008). Summation and quantity judgments of sequentially presented sets by capuchin monkeys *(Cebus apella)*. *American Journal of Primatology*, 70(2), 191–194.

Beran, M. J., McIntyre, J. M., Garland, A., & Evans, T. A. (2013). What counts for 'counting'? Chimpanzees, Pan troglodytes, respond appropriately to relevant and irrelevant information in a quantity judgment task. *Animal Behaviour*, 85(5), 987–993.

Beran, M. J., & Parrish, A. E. (2016). Capuchin monkeys *(Cebus apella)* treat small and large numbers of items similarly during a relative quantity judgment task. *Psychonomic Bulletin and Review*, 23(4), 1206–1213.

Boysen, S. T., & Berntson, G. G. (1989). Numerical competence in a chimpanzee *(Pan troglodytes)*. *Journal of Comparative Psychology*, 103(1), 23–31.

Call, J. (2000). Estimating and operating on discrete quantities in orangutans *(Pongo pygmaeus)*. *Journal of Comparative Psychology*, 114(2), 136–147.

Charles, E. P., & Rivera, S. M. (2009). Object permanence and method of disappearance: Looking measures further contradict reaching measures. *Developmental Science*, 12(6), 991–1006.

Cosmides, L., & Tooby, J. (1996). Are humans good intuitive statisticians after all? Rethinking some conclusions from the literature on judgment under uncertainty. *Cognition*, 58(1), 1–73.

Dacke, M., & Srinivasan, M. V. (2008). Evidence for counting in insects. *Animal Cognition*, 11(4), 683–689.

Davis, H. (1984). Discrimination of the number three by a raccoon. *Animal Learning & Behavior*, 12, 409–413.

Denison, S., Reed, C., & Xu, F. (2013). The emergence of probabilistic reasoning in very young infants: Evidence from 4.5- and 6-month-olds. *Developmental Psychology*, 49(2), 243–249.

Denison, S., Trikutam, P., & Xu, F. (2014). Probability versus representativeness in infancy: Can infants use naive physics to adjust population base rates in probabilistic inference? *Developmental Psychology*, 50(8), 2009–2019.

Denison, S., & Xu, F. (2010a). Integrating physical constraints in statistical inference by 11-month-old infants. *Cognitive Science*, 34(5), 885–908.

Denison, S., & Xu, F. (2010b). Twelve- to 14-month-old infants can predict single-event probability with large set sizes. *Developmental Science*, 13(5), 798–803.

Denison, S., & Xu, F. (2012). Probabilistic inference in human infants. *Advances in Child Development and Behavior*, 43, 27–58.

Denison, S., & Xu, F. (2014). The origins of probabilistic inference in human infants. *Cognition*, 130(3), 335–347.

Drucker, C. B., Rossa, M. A., & Brannon, E. M. (2016). Comparison of discrete ratios by rhesus macaques *(Macaca mulatta)*. *Animal Cognition*, 19(1), 75–89.

Farnsworth, G. L., & Smolinski, J. L. (2006). Numerical discrimination by wild northern mockingbirds. *Condor*, 108(4), 953–957.

Feigenson, L., Carey, S., & Hauser, M. (2002). The representations underlying infants' choice of more: Object files versus analog magnitudes. *Psychological Science*, 13(2), 150–156.

Feigenson, L., Dehaene, S., & Spelke, E. (2004). Core systems of number. *Trends in Cognitive Sciences*, 8(7), 307–314.

Geary, D. C., Berch, B. B., & Mann Koepke, K. (2015). The evolution of number systems. In D. C. Geary, D. B. Berch, & K. M. Koepke (Eds.), *Evolutionary origins and early development of number processing* (pp. 335–353). San Diego, CA: Academic Press.

Hamilton I. M., (2010). Foraging theory. In D. F. Westneat, & C. W. Fox, (Eds.), *Evolutionary behavioral ecology* (pp. 177–193). New York: Oxford University Press.

Hanus, D., & Call, J. (2007). Discrete quantity judgments in the great apes *(Pan paniscus, Pan troglodytes, Gorilla gorilla, Pongo pygmaeus)*: The effect of presenting whole sets versus item-by-item. *Journal of Comparative Psychology*, 121(3), 241–249.

Hanus, D., & Call, J. (2014). When maths trumps logic: Probabilistic judgements in chimpanzees. *Biological Letters*, 10, 20140892. https://doi.org/10.1098/rsbl.2014.0892

Holland, P. W. (1986). Statistics and causal inference. *Journal of the American Statistical Association*, 81(396), 945–960.

Hunt, S., Low, J., & Burns, K. C. (2008). Adaptive numerical competency in a food-hoarding songbird. *Proceedings of the Royal Society B: Biological Sciences*, 275(1649), 2373–2379.

McComb, K., Packer, C., & Pusey, A. (1994). Roaring and numerical assessment in contests between groups of female lions, *Panthera leo*. *Animal Behaviour*, 47(2), 379–387.

McCrink, K., & Wynn, K. (2007). Ratio abstraction by 6-month-old infants. *Psychological Science*, 18, 740–745. https://doi.org/10.1111/j.1467-9280.2007.01969.x

Navarro D. J. (2015). *Learning statistics with R: A tutorial for psychology students and other beginners (Version 0.5)*. Adelaide, Australia: University of Adelaide.

Nieder, A. (2005). Counting on neurons: The neurobiology of numerical competence. *Nature Reviews Neuroscience*, 6(3), 177–190.

Perdue, B. M., Talbot, C. F., Stone, A. M., & Beran, M. J. (2012). Putting the elephant back in the herd: Relative quantity judgments match those of other species. *Animal Cognition*, 15, 955–961.

Piaget J., & Inhelder B. (1975). *The origin of the idea of chance in children*. New York: Norton, (p. 251).

Pisa, P., & Agrillo, C. (2009). Quantity discrimination in felines: A preliminary investigation of the domestic cat *(Felis silvestris catus)*. *Journal of Ethology*, 27(2), 289–293.

Potrich, D., Sovrano, V. A., Stancher, G., & Vallortigara, G. (2015). Quantity discrimination by zebrafish *(Danio rerio)*. *Journal of Comparative Psychology*, 129(4), 388–393.

Povinelli, D. J. (2000). *Folk physics for apes: The chimpanzee's theory of how the world works*. Oxford University Press, Oxford: New York.

R Core Team, 2014. A language and environment for statistical computing. R Foundation for Statistical Computing, Vienna, Austria.

Rakoczy, H., Clüver, A., & Saucke, L., Stoffregen, N., Grabener, A., Migura, J., & Call, J. (2014). Apes are intuitive statisticians. *Cognition*, 131(1), 60–68.

Reznikova, Z., & Ryabko, B. (2011). Numerical competence in animals, with an insight from ants. *Behaviour*, 148(4), 405–434.

Rugani, R., Cavazzana, A., Vallortigara, G., & Regolin, L. (2013). One, two, three, four, or is there something more? Numerical discrimination in day-old domestic chicks. *Animal Cognition*, 16(4), 557–564.

Seed, A., Seddon, E., Greene, B., & Call, J. (2012). Chimpanzee 'folk physics': bringing failures into focus. *Philosophical Transactions of the Royal Society B Biological Sciences*, 367, 2743–2752. https://doi.org/10.1098/rstb.2012.0222

Shinskey, J. L., & Munakata, Y. (2005). Familiarity breeds searching — Infants reverse their novelty preferences when reaching for hidden objects. *Psychological Science*, 16(8), 596–600.

Skyrms B. (1975). *Choice and chance: An introduction to inductive logic*. Encino, CA: Dickenson Pub, (p. 220).

Tecwyn, E. C., Denison, S., Messer, E. J., & Buchsbaum, D. (2016). Intuitive probabilistic inference in capuchin monkeys. *Animal Cognition*, 130(3), 335–347.

Téglás, E., Girotto, V., Gonzalez, M., & Bonatti, L. L. (2007). Intuitions of probabilities shape expectations about the future at 12 months and beyond. *Proceedings of the National Academy of Sciences USA*, 104(48), 19156–19159.

Téglás, E., Vul, E., Girotto, V., Gonzalez, M., Tenenbaum, J. B., & Bonatti, L. L. (2011). Pure reasoning in 12-month-old infants as probabilistic inference. *Science*, 332(6033), 1054–1059.

Tenenbaum, J. B., Griffiths, T. L., & Kemp, C. (2006). Theory-based Bayesian models of inductive learning and reasoning. *Trends in Cognitive Sciences*, 10(7), 309–318.

Tversky, A., & Kahneman, D. (1974). Judgment under Uncertainty—Heuristics and biases. *Science*, 185(4157), 1124–1131.

Tversky, A., & Kahneman, D. (1981). The framing of decisions and the psychology of choice. *Science*, 211(4481), 453–458.

Vonk, J., & Beran, M. J. (2012). Bears "count" too: Quantity estimation and comparison in black bears, *Ursus americanus*. *Animal Behaviour*, 84, 231–238.

Völter, C. J., & Call, J. (2017). Causal and inferential reasoning in animals. In G. M. Burghardt, I. M. Pepperberg, C. T. Snowdon, & T. Zentall (Eds.), APA handbook of comparative psychology Vol 2: Perception, learning, and cognition (pp. 643–671). US: American Psychological Association.

Ward, C., & Smuts, B. B. (2007). Quantity-based judgments in the domestic dog *(Canis lupus familiaris)*. *Animal Cognition*, 10(1), 71–80.

Wilson, M. L., Britton, N. F., & Franks, N. R. (2002). Chimpanzees and the mathematics of battle. *Proceedings of the Royal Society of London B Biological Sciences*, 269, 1107–1112.

Xu, F., & Denison, S. (2009). Statistical inference and sensitivity to sampling in 11-month-old infants. *Cognition*, 112, 97–104.

Xu, F., & Garcia, V. (2008). Intuitive statistics by 8-month-old infants. *Proceedings of the National Academy of Sciences USA*, 105(13), 5012–5015.

SUPPORTING INFORMATION

Additional Supporting Information may be found online in the supporting information tab for this article.